Hardy Weinberg Problem Set

\[ p^2 + 2pq + q^2 = 1 \] and \( p + q = 1 \)
\( p = \) frequency of the dominant allele in the population
\( q = \) frequency of the recessive allele in the population
\( p^2 = \) percentage of homozygous dominant individuals
\( q^2 = \) percentage of homozygous recessive individuals
\( 2pq = \) percentage of heterozygous individuals

1. View the Dragons below. The winged trait is dominant.

\[
\begin{align*}
q^2 \text{ (aa)} &= 0.33 \\
q \text{ (a)} &= 0.57 \\
p \text{ (A)} &= 0.43 \\
p^2 \text{ (AA)} &= 0.18 \\
2pq \text{ (Aa)} &= 0.49
\end{align*}
\]

What is the frequency of heterozygote dragons in your population?

0.49
2. You have sampled a population in which you know that the percentage of the homozygous recessive genotype (aa) is 36%. Using that 36%, calculate the following:
   A. The frequency of the "aa" genotype.
   B. The frequency of the "a" allele.
   C. The frequency of the "A" allele.
   D. The frequencies of the genotypes "AA" and "Aa."
   E. The frequencies of the two possible phenotypes if "A" is completely dominant over "a."

   \[ A- 0.36 \quad aa 0.36 \quad Aa 0.48 \quad a=0.6 \]

3. There are 100 students in a class. Ninety-six did well in the course whereas four blew it totally and received a grade of F. Sorry. In the highly unlikely event that these traits are genetic rather than environmental, if these traits involve dominant and recessive alleles, and if the four (4%) represent the frequency of the homozygous recessive condition, please calculate the following:
   A. The frequency of the recessive allele.
   B. The frequency of the dominant allele.
   C. The frequency of heterozygous individuals.

   \[ p=0.37 \quad q=0.63 \]

4. Within a population of butterflies, the color brown (B) is dominant over the color white (b). And, 40% of all butterflies are white. Given this simple information, which is something that is very likely to be on an exam, calculate the following:
   A. The percentage of butterflies in the population that are heterozygous.
   B. The frequency of homozygous dominant individuals.

   \[ 2(0.37)(0.63)=0.417 \]

5. After graduation, you and 19 of your closest friends (lets say 10 males and 10 females) charter a plane to go on a round-the-world tour. Unfortunately, you all crash land (safely) on a deserted island. No one finds you and you start a new population totally isolated from the rest of the world. Two of your friends carry (i.e. are heterozygous for) the recessive cystic fibrosis allele (c). Assuming that the frequency of this allele does not change as the population grows, what will be the incidence of cystic fibrosis on your island?

   \[ 0.025 \quad 0.25 \quad q \]

6. Cystic fibrosis is a recessive condition that affects about 1 in 2,500 babies in the Caucasian population of the United States. Please calculate the following.
   The frequency of the recessive allele in the population.
   The frequency of the dominant allele in the population.
   The percentage of heterozygous individuals (carriers) in the population.

   \[ 0.02 \quad 0.96 \quad 0.039 \]

7. This is a classic data set on wing coloration in the scarlet tiger moth (Panaxia dominula). Coloration in this species had been previously shown to behave as a single-locus, two-allele system with incomplete dominance. Data for 1612 individuals are given below:

   White-spotted (AA) = 1469 Intermediate (Aa) = 138 Little spotting (aa) = 5

Calculate the allele frequencies (p and q)

   \[ p=0.944 \quad q=0.056 \]

8. The allele for a widow's peak (hairline) is dominant over the allele for a straight hairline. In a population of 500 individuals, 25% show the recessive phenotype. How many individuals would you expect to be homozygous dominant and heterozygous for the trait?

   \[ \frac{2}{5} q^2 = 0.25 \quad q = 0.5 \]

   \[ 2(0.5)(0.5) \]

   \[ 0.5 \]

   \[ 250 \]
The allele for a hitchhiker's thumb is recessive compared to straight thumbs, which are dominant. In a population of 1000 individuals, 510 show the dominant phenotype. How many individuals would you expect for each of the three possible genotypes for this trait?

\[\begin{array}{ccc}
Q^2 & p^2 & q^2 \\
460 & 420 & 120 \\
\end{array}\]

\[\frac{7p^2 + 2pq + 5q^2}{1000} \approx 0.51\]

10. REAL WORLD APPLICATION PROBLEM

Choose a human trait to study and survey a population at your school. (Aim for at least a sample size of 50 to get meaningful results). Use your sample to determine the allele frequencies in the human population.

Traits (dominant listed first)

- Hitchhiker's Thumb vs Straight Thumbs
- Widow's peak vs straight hairline
- PTC taster vs non-taster
- Short Big toe vs long big toe
- Free earlobes vs attached earlobes
- Tongue rolling vs non-rolling
- Bent little fingers vs straight little fingers
- Arm crossing (left over right) vs right over left
- Ear points vs no ear points